# The Low Entropy Conjecture: The challenges of Modern Irish nominal declension

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# The Paradigm Cell Filling Problem

Speakers of languages with complex morphology and multiple inflection classes must generalize beyond direct experience, since it's implausible to imagine they will have encountered each form of every word

**Paradigm Cell Filling Problem**: Given exposure to an inflected wordform of a novel lexeme, what licenses reliable inferences about the other wordforms in its inflectional family? (Ackerman, Blevins, & Malouf 2009)

### Some questions

- 1. How are wordforms organized into patterns within a morphological system?
- 2. How can one identify implicative relations between these units?
- 3. How might the implicative organization of a system contribute to licensing inferences that solve the paradigm cell filling problem?
- 4. How does this organization, and the surface inferences it licenses, contribute to the robustness and learnability of complex morphological systems?

# The basic background

Inflectional morphology can exhibit spectacular complexity in:

- i. syntagmatic, morphophonemic, suprasegmental structure of individual words;
- ii. the size of inventories for morphosyntactic distinctions formall expressed by words;
- iii. paradigmatic patterns that (classes of) words participate in.

This is the **External Complexity** or **E-complexity** of a morphological system

# Our guiding intuition

Morphological systems **must** be simple in ways that allow them to be learned and used by native speakers, irrespective of how complex words and paradigms may appear according to external measures.

Speakers must generalize beyond their direct experience:

Morphological systems must permit speakers to make accurate guesses about unknown forms of lexemes based on only a few known forms.

This is the **Internal Simplicity** or **I-simplicity** of a system

# Our hypothesis: I-simplicity

I-simplicity is measurable and quantifiable

**Principle of Low Paradigm Entropy**: Paradigms tend to have low expected conditional entropy, where Paradigm entropy is the average of conditional entropies among all pairs of words.

Gradation in first declension nouns in Saami (Bartens 1989:511)

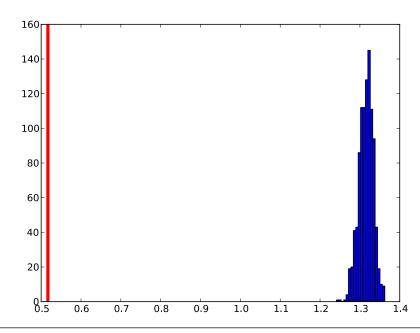
	'Wea	akening'	'Stren	gthening'
	Sing	Plu	Sing	Plu
Nominative	bihttá	bihtát	baste	basttet
Gen/Acc	bihtá	bihtáid	bastte	basttiid
Illative	bihttái	bihtáide	bastii	basttiide
Locative	bihtás	bihtáin	basttes	basttiin
Comitative	bihtáin	bihtáiguin	basttiin	basttiiguin
Essive		bihttán		basten
		'piece'		'spoon'

$$H(\text{loc.pl}|\text{nom.sg}) = H(\text{nom.sg, loc.pl}) - H(\text{nom.sg})$$
  
= 1.0 - 1.0  
= 0.0

# Results based on uniform type freqs

Language	Declensions	Cells	Realizations	Paradigm	Bootstap	Bootstrap
				entropy	Avg	p
Arapesh	26	2	41	0.630	0.630	1.000
Burmeso	2	12	24	0.000	0.000	1.000
Fur	19	12	80	0.517	1.316	0.001
Kwerba	4	12	26	0.428	0.523	0.001
Ngiti	10	16	68	0.484	1.019	0.001
Nuer	16	6	12	0.793	0.811	0.160
Russian	4	12	26	0.538	0.541	0.383

Fur



# Upper bounds from idealized data

Bonami et. al. (2011), Sims (2011 LSA Institute) point out the challenges for testing the Low Entropy Conjecture beyond using grammar descriptions:

#### Realistic data bases:

- 1. Need for veridical representations of spoken words, rather than phonological idealizations.
- 2. Need for type and token frequencies
- 3. Need to recognize small, reliable implicational patterns that partition the whole paradigm into sub-paradigms

# A passing effort: Tundra Nenets

"Given any Tundra Nenets inflected nominal word form, what are the remaining 209 forms of this lexeme for the allowable morphosyntactic feature property combinations CASE: {nom, acc, gen, dat, loc, abl, pro}, NUMBER: {singular, dual, plural}, POSSESSOR: {3 persons 3 numbers}?"

Corpus of 4,334 nominals with type and token frequencies

Nom Sg|Acc Pl; Acc Pl|Nom Sg

Nom Sg	Acc PI	
ngano	nganu	'boat'
lyabtu	lyabtu	'harnessed deer'
ngum	nguwo	'grass'
xa	xawo	'ear'
nyum	nyubye	'name'
yí	yíbye	'wit'
myir	myirye	'ware'
wí′	wíngo	'tundra'
we'	weno	'dog'
nguda	ngudyi	'hand'
xoba	xob	'fur'
sawənye	sawənyi	'magpie'
tyírtya	tyírtya	'bird'

#### **Modern Irish nominal inflection**

Modern Irish presents a challenging test case for the Low Entropy Conjecture

Definite nominal paradigm (excluding vocative):

caibidil	'chapter'	an chaibidil	DEF.COM.SG
		na caibidle	DEF.GEN.SG
		an gcaibidil	DEF.PREP.SG
		na caibidlí	DEF.COM.PL
		na gcaibidlí	DEF.GEN.PL
		na caibidlí	DEF.PREP.PL

Definiteness, case, and number marked by an article, prefix, consonant mutation, stem alternation, syncope, and/or suffix

"This kind of complexity makes students, teachers, and linguists alike scratch their heads in wonder and fear." (Carnie 2008, 6)

#### **Modern Irish nominal inflection**

Carnie (2008) presents an updated and elaborated analysis of the nominal system

- Two genders
- Forty singular declensions
- Sixty-five plural types

Carnie also gives class membership and full paradigms for 1,216 nouns, exemplifying 220 gender/declension/plural class combinations

This gives us a detailed inventory of inflection classes, with information about the realization of wordforms, and from the word list we can estimate the type frequency of each

Paradigm entropy = 1.529 bits (!)

H(col row)	COM.SG	GEN.SG	PREP.SG	COM.PL	GEN.PL	PREP.PL	E[ROW]
COM.SG		2.955	0.034	3.936	3.690	3.936	2.910
GEN.SG	0.000		0.021	2.089	2.055	2.089	1.251
PREP.SG	0.000	2.942		3.926	3.680	3.926	2.895
COM.PL	0.625	1.733	0.649		0.003	0.000	0.602
GEN.PL	0.795	2.116	0.819	0.419		0.419	0.914
PREP.PL	0.625	1.733	0.649	0.000	0.003		0.602
E[COL]	0.409	2.296	0.434	2.074	1.886	2.074	1.529

GEN.SG as a principal part

H(col row)	COM.SG	GEN.SG	PREP.SG	COM.PL	GEN.PL	PREP.PL	E[ROW]
COM.SG		2.955	0.034	3.936	3.690	3.936	2.910
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Plurals are mostly inter-predictable

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Singular forms are very bad predictors of plural forms

H(col row)	COM.SG	GEN.SG	PREP.SG	COM.PL	GEN.PL	PREP.PL	E[ROW]
COM.SG		2.955	0.034	3.936	3.690	3.936	2.910
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#### Some reasons to doubt

Inflection class analysis based on a long philological tradition

Classes are based on the standard written language, but Modern Irish orthography is not very transparent

neamhthruamhéalach /n<sup>j</sup>auhruav<sup>j</sup>eːlah/

Consonant mutations are not easy to identify in spoken forms

```
'boat' an bád /ən baːd/ COM.SG
an mbád /ən maːd/ PREP.SG

'bag' an mála /ən maːlə/ COM.SG
an mála /ən maːlə/ PREP.SG
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Classes often restricted to particular genders, phonological patterns, semantic patterns, etc.

#### An alternative

Declension systems like Carnie's aren't designed for answering the questions we're asking

A better alternative (for this task) is to derive the classes directly from the lexicon

Ideally, we would find all and only the patterns that obtain in the lexicon, without coming at the descriptive problem with any prior assumptions

But this is very difficult (and likely impossible in principle)

The first step is to convert Carnie's paradigms into a phonological transcription using TCD's Abair speech synthesis system

caibidil	'chapter'	/kab <sup>j</sup> əd <sup>j</sup> əl <sup>j</sup> /
an chaibidil	DEF.COM.SG	/ənxab <sup>j</sup> id <sup>j</sup> il <sup>j</sup> /
na caibidle	DEF.GEN.SG	/nəkab <sup>j</sup> id <sup>j</sup> l <sup>j</sup> ə/
an gcaibidil	DEF.PREP.SG	/əngab <sup>j</sup> id <sup>j</sup> il <sup>j</sup> /
na caibidlí	DEF.COM.PL	/nəkab <sup>j</sup> id <sup>j</sup> l <sup>j</sup> iː/
na gcaibidlí	DEF.GEN.PL	/nəgab <sup>j</sup> id <sup>j</sup> l <sup>j</sup> iː/
na caibidlí	DEF.PREP.PL	/nəkab <sup>j</sup> id <sup>j</sup> l <sup>j</sup> iː/

Perform a multiple alignment using modified edit distance

Remove anything that stays constant across the paradigm to find the signature of this lexeme's inflection class

	k	Э	ə	
ən	X	i	i	
nə	k	i	Ø	ə
ən	g	i	i	
nə	k	i	Ø	iː
nə	g	i	Ø	iː
nə	k	i	Ø	iː

Applying this discovery procedure yields 950 declensions (not very useful for pedagogy!)

These 'classes' are essentially small phonological neighborhoods, which serve as the domains for analogies

A nagging concern: many of the neighborhoods are very small (consisting of a single lexeme in the 1,200 word sample) and may not reflect any useful generalizations

#### Next steps

- Look at larger neighborhoods, perhaps by using a feature representation for segments
- Scale up to a larger sample of nouns, to see how neighborhoods fill in

#### Much lower paradigm entropy

H(col row)	COM.SG	GEN.SG	PREP.SG	COM.PL	GEN.PL	PREP.PL	E[ROW]
COM.SG		1.003	0.808	0.976	0.104	1.011	0.780
GEN.SG	0.723		0.840	0.039	0.602	0.010	0.443
PREP.SG	0.304	0.617		0.594	0.110	0.622	0.449
COM.PL	0.770	0.113	0.892		0.603	0.123	0.500
GEN.PL	0.467	1.245	0.976	1.172		1.250	1.022
PREP.PL	0.724	0.003	0.838	0.041	0.600		0.441
E[COL]	0.598	0.596	0.871	0.565	0.404	0.603	0.606

GEN.SG is still very predictive, but it's not quite a 'principal part'

H(col row)	COM.SG	GEN.SG	PREP.SG	COM.PL	GEN.PL	PREP.PL	E[ROW]
COM.SG		1.003	0.808	0.976	0.104	1.011	0.780
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Conditional entropies are more even overall

Most forms are mostly predictable from most other forms, with no one form as the key

Singular forms are reasonably good predictors of plural forms

H(col row)	COM.SG	GEN.SG	PREP.SG	COM.PL	GEN.PL	PREP.PL	E[ROW]
COM.SG		1.003	0.808	0.976	0.104	1.011	0.780
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# **Token frequency**

All reported entropy calculations were weighted by **type** frequency (the number of lexemes in each class)

The **token** frequency of each inflected form may also be relevant for learning

Form	Predicting	Predicted	Frequency*
COM.SG	0.780	0.598	155,960
GEN.SG	0.443	0.596	71,614
PREP.SG	0.449	0.871	161,699
COM.PL	0.500	0.565	31,711
GEN.PL	1.022	0.404	22,660
PREP.PL	0.441	0.603	40,794

#### **Conclusions**

While detailed descriptive accounts of morphological systems can provide a useful **entry point** for analysis, they can also lead, as in Carnie's fine description of Irish nominal declension, to misleading conclusions about Paradigm Entropy (Bonami et. al. 2011).

In order to explore the validity of the Low Entropy Conjecture as well as the numerous ways that it may obtain in morphological systems, the choice of **representation** (for both forms and classes) crucial

Including accurate type (and token?) **frequency** is also important for getting an accurate picture of lexical organization

Paraphrasing Bonami et. al. (2011): this is "tedious work", but it's both doable and necessary if we really want to understand morphological systems.

#### Sources

Farrell Ackerman et.al. 2009. "Parts and whole: Implicative patterns in inflectional paradigms." In J. P. Blevins & J. Blevins eds. *Analogy in Grammar*. Oxford University Press.

Olivier Bonami et. al. 2011. Measuring inflection complexity. Presented at Quantitative Methods in Morphology Workshop, Center for Human Development, UCSD.

Andrew Carnie. 2008. Irish Nouns: A Reference Guide. Oxford University Press.

Amelia Kelly. Text-to-Speech Synthesis for Irish. Presented at University of Amsterdam, February 2009. <a href="http://abair.ie">http://abair.ie</a>

Adam Kilgarriff, Michael Rundell and Elaine Uí Dhonnchadha. 2006. "Efficient corpus development for lexicography: Building the New Corpus for Ireland." *Language Resources and Evaluation* 40(2):127–152. <a href="http://corpas.focloir.ie">http://corpas.focloir.ie</a>/ [via Michal Boleslav Měchura]

Andrea Sims. 2011. Information theory and paradigmatic morphology. Presentation at Information-theoretic Approaches to Linguistics Workshop LSA Summer Institute, Bolder, Colorado.